Study Guide 2
A)

MATH 140 Lab: Section 1
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Student's ID:
Note: This study guide contains my practice questions that I think will be useful for preparing you for the second exam in Calculus for Life Scientists.

Question 1: Find the derivative for the following:
Hint: Use Implicit Differentiation to find $y^{\prime}$

$$
e^{y}+x y^{3}=5 x
$$

Question 2: Find the equation of the tangent line at the point $(0, \pi)$ to the following curve:

$$
x^{2} \cos ^{2} y-\sin y=-x
$$

Question 3: Determine the values of $x$ for which the function:

$$
y=x^{5}-20 x^{2}+1
$$

is decreasing/increasing and determine concavity of the function. Find the location of maxima/minima and inflection points. Sketch the curve.

Question 4: Find the absolute extrema of the given function on $[-3,2]$.

$$
f(x)=x^{3}-3 x+1
$$

Question 5: Given a function:

$$
f(x)=e^{-\frac{x^{2}}{2}}
$$

Determine the intervals where the graph of $f$ is concave up and concave down, then find the inflection points.

Question 6: Find the integral for the following:
a. $\int \frac{4 x}{x^{2}+3} d x$
b. $\int\left(3 e^{x}-2\right) d x$
c. $\int \frac{x^{\frac{1}{3}}-3}{x^{\frac{2}{3}}} d x$
d. $\int 2 \sec x \tan x d x$

Question 7: Evaluate the integral:

$$
\int x^{-3}\left(\sqrt[3]{x}-3 x^{-1}+3\right) d x
$$

Question 8: Evaluate the integral:

$$
\int \frac{x^{3}}{\sqrt{1-x^{4}}} d x
$$

Question 9: Find the following integral:

$$
\int\left(\frac{8 x+2}{x}\right)^{2} d x
$$

Question 10: A rectangular plot of farmland will be bounded from one side by a river and from the other three sides by a fence. With a 2600 ft of the wire at your disposal. What is the largest area you can enclose?

