Quiz 7


## MATH 172 Lab: Sections 7 and 8

## Lab Instructor (TA): Mohammed Gabar



Student's Name: Mohammed Gabar
Student's ID: Solution
Note: This quiz covers parametric equations and polar coordinates.
Show your work and circle your answers. Neatness and organization count!
Question 1: (3 points) Find the equation and draw the curve for the following parametric equations: $x=5 \cos (t)$ and $y=2 \sin (t)$ where $0 \leq t \leq 2 \pi$.

Solution:

$$
\begin{aligned}
& x=5 \cos (t) \Longrightarrow \frac{x}{5}=\cos (t) \\
& y=2 \sin (t) \Longrightarrow \frac{y}{2}=\sin (t)
\end{aligned}
$$

$$
\begin{aligned}
& y=2 \sin (t) \Longrightarrow \frac{y}{2}=\sin (t) \\
& \text { Then, we use trig identity } \sin ^{2}(t)+\cos ^{2}(t)=1
\end{aligned}
$$

$$
\Rightarrow\left(\frac{x}{5}\right)^{2}+\left(\frac{y}{2}\right)^{2}=1
$$

$$
\Rightarrow \frac{x^{2}}{25}+\frac{y^{2}}{4}=1
$$



Question 2: (2 points) Find the rectangular coordinates for the following polar coordinates:

$$
r=6 \cos (\theta)
$$

Solutions
First, me multiply both sides by $r$, we obtain:

$$
\begin{aligned}
& r^{2}=6 r \cos (\theta) \\
& x^{2}+y^{2}=6 x \Rightarrow x^{2}-6 x+y^{2}=0 \text { by completing the square, } \\
& \text { we obtain: } x^{2}-6 x+9+y^{2}=0+9 \Rightarrow(x-3)^{2}+y^{2}=9 \text { Equation } \\
& \text { of circle centered }(3,0) \text { of radius }=3 \text {. }
\end{aligned}
$$

