# Department of Mathematics Moreno Valley College 

## Mathematics 52

Course ID: (27488)
Second Take-Home Midterm
Fall 2016
Dates: November $15^{\text {th }}, 2016$ and November $16^{\text {th }}, 2016$
Times: 8:00 AM - 10:05 AM and 2:00 PM - 4:05 PM

## Professor: Mohammed Kaabar

| P1 | P2 | P3 | P4 | P5 | P6 | P7 | P8 | P9 | EC | Total |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 20 | 10 | $\mathbf{1 0}$ | $\mathbf{1 0}$ | $\mathbf{1 0}$ | $\mathbf{1 0}$ | $\mathbf{1 0}$ | $\mathbf{1 0}$ | $\mathbf{1 0}$ | $\mathbf{5}$ | $\mathbf{1 0 0}$ |
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## Student Name:

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## Student ID:

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## Exam Instructions:

1- This exam has 8 questions and two extra credit questions.
2- Make sure you answer all questions.
3- Cheating $=$ " $F$ "
4- Make sure to include this page in your submission materials.

Problem 1 (20 points): Determine whether the following is TRUE or FALSE and if it is false EXPLAIN why:
a. Linear inequality is a mathematical statement that has a mathematical expression that is greater than only.
b. The solution for $-5+7 x<3 x+7$ is $3>x$.
c. The solution for $\left(\frac{4 z+5}{2}-\frac{1}{3}\right) \geq\left(-\frac{7}{2}+z\right)$ is $z \leq-\frac{34}{6}$.
d. The general form of the interval notation can be written as $\{$ variable|solution $\}$.
e. $(0,2)$ is located on the first quadrant only.
f. $(-1,2)$ is located on the second quadrant.
g. Given that $l_{1}$ and $l_{2}$ are non-vertical lines. If $l_{1} \| l_{2}$, then $m_{1}+m_{2}=-1$.
h. Given that $l_{1}$ and $l_{2}$ are non-vertical lines. If $l_{1}$ and $l_{2}$ make an angle of $90^{\circ}$, then $m_{1} \cdot m_{2}=-1$.
i. It is impossible to derive the slope-point form of equation of line using the slope formula by considering the slope passes through $\left(x_{1}, y_{1}\right)$ and $(x, y)$.
j. $\quad y$-intercept is defined as a point on the $y$-axis that is considered the passing point for the graph of equation: $y=m x+b$ so the $y$-interecept is $(b, 0)$.

Problem 2 ( $\mathbf{1 0}$ points): Answer each of the following:
a. What is the name of zero slope? $\qquad$
b. What is the name of undefined slope? $\qquad$
c. What is the positive slope? ----------------------------------------------------
d. Draw the positive slope:
e. What is the negative slope? $\qquad$
f. Draw the negative slope:
g. Derive the point-slope form of the equation of line:

Hint: Use $\left(x_{1}, y_{1}\right)$ and $(x, y)$ as two given points and write the slope formula $m=\frac{\left(y_{2}-y_{1}\right)}{\left(x_{2}-x_{1}\right)}$

Problem 3 ( 10 points): In our class, we talked about two theorems of lines: vertical line and horizontal line. Discuss those two theorems and make sure to include examples and graphs for both lines.

Hint: Use "Slope of a Line" lecture notes.

Problem 4 (10 points): In our class, we talked about two theorems of non-vertical lines:
Discuss those two theorems and make sure to include examples and graphs for both non-vertical lines.

Hint: Use "Slope of a Line" lecture notes.

Problem 5 (10 points): Solve TWO of the following FIVE problems:
1- Solve for $x$ given that $|-2 x+2|=3$.
2- Solve for $x$ given that $|5 x+12| \geq 6$.
3- A line passes through $(2,-1)$ and it is perpendicular to another line:
$2 y+3-5 y=-2 x+5 x$. Write the equation for this line.
4- Solve the following linear inequality:

$$
15 \beta+\sqrt[3]{8}<(-6766776.766)^{0}+2 \beta
$$

5- Solve the following linear inequality:

$$
-2 \beta+1^{\sqrt[3]{8}}<\left(-\frac{-23433.63}{-343544.12}\right)^{0}+12 \beta
$$

Problem 6 (10 points): Discussion Problems:
a. When we talked about dividing the polynomials, we mentioned that there are two methods of division: long and synthetic division. In addition, we talked about a common property for both of them and a limited property for synthetic division only. Discuss that in more details.
b. We talked about the properties of factoring, and I asked a question: Given that $a$ and $b$ are real numbers, then Is $(a-b)^{2}=a^{2}-b^{2}$ ???!!! Discuss that in more details.

Problem 7 ( 10 points): Use either long division or synthetic division to do the following:

$$
\frac{x^{3}+x^{2}-x-1}{x-3}
$$

Problem 8 (10 points): Factor each of the following:
a. $\left(x^{2}-12\right)$
b. $(x-25)$
c. $\left(16 a^{2}-48 a c+36 c^{2}-100\right)$
d. $\left(25 x^{2}-16\right)$
e. $\left(24 z^{2}-12\right)$

Problem 9 ( 10 points): Simplify each of the following:
a. $(2 x-1)^{2}$
b. $x^{3} y^{-1} z^{2} m^{2} y m^{-2} x^{-2}$
c. $\left(-\frac{x^{3}}{3 y^{2} x^{7}}\right)^{3}$
d. $\left(x^{2}+1\right)^{2}$
e. $7 y^{2} x^{3}\left(-3 x^{-3} y^{-5}\right)$

Extra Credit Problem (5 points): Use only synthetic division to do the following:

$$
\frac{x^{3}+x^{2}-x-1}{2 x^{2}-x+2}
$$



